## Chem 370 - Spring, 2019 Assignment 8 - Solutions

10.1 a. All tetrahedral complexes are high spin. For  $T_d d^6$  the configuration is  $e^3 t_2^3$ :

$$\frac{1}{1} \quad \frac{1}{1} \quad \frac{1}{1} \quad t_2 \\ \Rightarrow 4 \text{ unpaired electrons} \\ \frac{1}{1} \quad \frac{1}{1} \quad e$$

b.  $Co(H_2O)_6^{2+}$  is  $d^7$  high-spin  $O_h$  because  $H_2O$  is a weak-field ligand. (Do not confuse  $Co^{2+}$  with  $Co^{3+}$ , which tends to be low-spin, even with  $H_2O$ .)



d. Square planar complexes have the following splitting scheme, filled in a low-spin manner. (The middle two levels may be reversed in some cases, but that does not generally affect the overall configuration or number of unpaired electrons.)

$$\begin{array}{ccc} & & & & & \\ & & & & \\$$

- 10.2 a. To have  $M^{3+}$  with  $3d^{1}$ , the neutral atom would need to be  $3d^{2}4s^{2}$ , which is Ti.
  - b. The most unpaired electrons is  $d^5$ .  $[MBr_4]^-$  has a  $M^{3+}$  ion. These two facts make it Fe.
  - c. Diamagnetic  $[M(CN)_6]^{3-}$  would be a low-spin  $d^6$ , because  $CN^-$  is a high-field ligand. The  $M^{3+}$  ion with a  $3d^6$  configuration is Co.
  - d. If CFSE =  $-0.6\Delta_{o}$  with no pairing terms, there are no paired electrons. The high-spin configuration  $t_{2g}{}^{3}e_{g}{}^{1}$  would have a CFSE =  $(-0.4)(3)\Delta_{o} + (0.6)(1)\Delta_{o} = -0.6\Delta_{o}$ . This would be the configuration for Cr<sup>2+</sup>. If pairing energy is ignored, the configuration  $d^{9} = t_{2g}{}^{6}e_{g}{}^{3}$  would also fit this description, but with pairing energy CFSE =  $(-0.4)(6)\Delta_{o} + (0.6)(3)\Delta_{o} + 4P = -0.6 + 4P$ . This would be the configuration for Cu<sup>2+</sup>.

- 10.7 This is  $\{[\text{Fe}(\text{H}_2\text{O})_6]^{2+}\}_2\{[\text{Fe}(\text{CN})_6]^{4-}\}\)$ . The cation is high-spin  $d^6$  with  $\mu = 4.89$  B.M., and the anion is low-spin  $d^6$  with  $\mu = 0$ . Thus,  $\mu = (2/3)(4.89 \text{ B.M.}) = 3.27$ . For 2.67 electrons,  $\mu = \sqrt{n(n + 2)} = \sqrt{(2.67)(4.67)} = 3.53$ , which is close to the expected average of two paramagnetic cations and one diamagnetic anion.
- 10.8  $\text{Co}^{2+}$  is  $d^7$ . Tetrahedral would be 3 unpaired electrons with  $\mu = 3.87$  B.M. Octahedral high-spin would also be 3 unpaired electrons with  $\mu = 3.87$  B.M. Square planar would be 1 unpaired electron with  $\mu = 1.73$  B.M. A  $d^7$  low-spin octahedral complex would also be 1 unpaired electron with  $\mu = 1.73$  B.M.
- 10.21 a. When compression occurs on the *z* axis, those orbitals with a *z* component  $(d_{xz}, d_{yz}, d_{z^2})$  are destabilized, and those with an *xy* component  $(d_{xy}, d_{x^2-y^2})$  are stabilized. The degeneracies of  $O_h$  are split on descent to  $D_{4h}$ . The effect is the opposite of stretching along *z* (see below).
  - b. Stretching along z destabilizes those orbitals with an xy component  $(d_{xy}, d_{x^2-y^2})$  and stabilizes those orbitals with a z component  $(d_{xz}, d_{yz}, d_{z^2})$ . The splitting of the octahedral  $t_{2g}$  and  $e_g$  levels is shown below.



10.23 a. The answers below also include the pairing energy (*P*) contributions, which the authors ignore in their answers (as do many other sources). Each electron in a  $t_{2g}$  orbital contributes  $-0.4\Delta_0$  to CFSE, and each electron in an  $e_g$  orbital contributes +0.6 to CFSE.

Complex	Config.	n	$\mu \left( B.M.\right)$	CFSE
$[Co(CO)_4]^-$	$d^{10}$	0	0	0
$[Cr(CN)_{6}]^{4-}$	$t_{2g}^{4}$	2	2.83	$-1.6\Delta_{o} + P$
$[Fe(H_2O)_6]^{3+}$	$t_{2g}^{3}e_{g}^{2}$	5	5.92	0
[Co(NO <sub>2</sub> ) <sub>6</sub> ] <sup>4-</sup> *	$t_{2g}^{6}e_{g}^{1}$	1	1.73	$-1.8\Delta_{o} + 3P$
$[Co(NH_3)_6]^{3+}$	$t_{2g}^{6}$	0	0	$-2.4\Delta_{o} + 3P$
$MnO_4^-$	$d^{0}$	0	0	0
$[Cu(H_2O)_6]^{2+}$	$t_{2g}^{6}e_{g}^{3}$	1	1.73	$-0.6\Delta_{\rm o} + 4P$

- \* The authors' answer book has  $[Co(NO_2)_6]^{4-}$  as a high-spin  $d^7$  case, but from the position of  $NO_2^-$  in the spectrochemical series you would predict this to be low-spin with 1 unpaired electron, as shown here.
- b. Both  $[Co(CO)_4]^-$  and  $MnO_4^-$  have no CFSE. The octahedral ions (except  $[Fe(H_2O)_6]^{3+}$ ) have CFSE values that favor octahedral coordination. The tetrahedral ions are stabilized by  $\pi$  bonding, with CO as an acceptor and O<sup>2-</sup> as a donor. Fe<sup>3+</sup> would have no CFSE, either as an octahedral or tetrahedral complex.
- c. Compare the CFSE values (ignoring pairing). Recall that  $\Delta_t = (4/9)\Delta_0$ .

Ion	Spin State	$O_h$ CFSE	$T_d$ CFSE
Co(II)	$d^7$ high spin	$-0.8\Delta_{o}$	$-1.2\Delta_{\rm t} = (4/9)(-1.2)\Delta_{\rm o} = -0.53\Delta_{\rm o}$
Ni(II)	$d^8$	$-1.2\Delta_{o}$	$-0.8\Delta_{\rm t} = (4/9)(-0.8)\Delta_{\rm o} = -0.36\Delta_{\rm o}$

As these results show, for Co(II)  $O_h$  CFSE is better than  $T_d$  CFSE by only  $0.27\Delta_o$ . For Ni(II),  $O_h$  CFSE is better by  $0.84\Delta_o$ . The smaller octahedral advantage with Co(II) makes it more likely that tetrahedral complexes may be stable, whereas with Ni(II) the octahedral advantage is so great that tetrahedral complexes are less likely.

## 10.26 a. A square pyramid is $C_{4\nu}$ .

From the direct product transformation properties listed in the  $C_{4\nu}$  character table, we can determine that the five-fold degeneracy among *d* orbitals in the free ion is lifted as follows:

$$d_{z^2} = a_1$$
  $d_{x^2-y^2} = b_1$   $d_{xy} = b_2$   $(d_{xz}, d_{yz}) = e$ 

The  $d_{xy}$  orbital is lowest, because its lobes lie between ligands, which are actually in a plane below. The degenerate  $(d_{xz}, d_{yz})$  orbitals with their lobes oriented between all ligands are next in order. The  $d_{z^2}$  orbital is next higher in energy, because it points directly at the axial ligand and its annular part is in the *xy* plane. The  $d_{x^2-y^2}$  orbital is the highest in energy, because its lobes point directly at the four basal ligands. The following CFT splitting scheme results:

$$\begin{array}{cccc} & & & \\ & &$$

With the preceding CFT results, we can construct an MO scheme, using five  $\sigma$ -SALCs from the ligands to interact with the *d* orbitals, whose symmetries we have already determined.

$C_{4v}$	Ε	$2C_4$	$C_2$	$2\sigma_v$	$2\sigma_d$		
$\Gamma_{\sigma}$	5	1	1	3	1	Σ	Σ/8
$A_1$	5	2	1	6	2	16	2
$A_2$	5	2	1	-6	-2	0	0
$B_1$	5	-2	1	6	-2	8	1
$B_2$	5	-2	1	-6	2	0	0
Ε	10	0	-2	0	0	8	1

$$\Gamma_{\sigma} = 2A_1 + B_1 + E$$

All SALCs have same-symmetry matches with d orbital symmetries and will form bonding and antibonding MOs. There are two  $A_1$  SALCs and only one  $A_1$  AO ( $d_2$ ), so we can form only three MOs of this symmetry. For simplicity, the scheme below assumes two bonding and one mixed antibonding MO. We do not have a  $B_2$  symmetry SALC, so the  $d_{xy}$  AO on the metal will be nonbonding. Electron pairs from the five ligands will fill the bonding MOs. Electrons from the metal will result in partial filling of the nonbonding  $b_2$  MO, then the antibonding e MO, the antibonding  $a_1$  MO, and finally the antibonding  $b_1$  MO, depending on the metal ion's  $d^n$ configuration. There is no simple way of predicting the order of the bonding MOs, so the order shown below is just a reasonable guess. However, as seen with octahedral and tetrahedral cases, the ordering of MOs filled from metal electrons is the same as predicted by CFT considerations.



Note that the pattern of electron filling in MOs beyond the five pairs from the ligands is the same as the order we deduced for the CFT *d*-orbital splitting (above). In the MO model, however, the lowest of these is a nonbonding level and the others are antibonding levels.

b. A pentagonal bipyramid is  $D_{5h}$ .



From the direct product transformation properties listed in the  $D_{5h}$  character table, we can determine that the five-fold degeneracy among *d* orbitals in the free ion is lifted as follows:

$$d_{z^2} = a_1'$$
  $(d_{x^2-y^2}, d_{xy}) = e_2'$   $(d_{xz}, d_{yz}) = e_1''$ 

The lobes of the degenerate  $d_{xz}$  and  $d_{yz}$  orbitals  $(e_1'')$  have no density in the *xy* plane (a nodal plane) and lie between the two axial positions. This makes them the most favorable (lowest energy) level in a CFT scheme. Conversely, the least favored (highest energy) pair would be the degenerate  $d_{x^2-y^2}$  and  $d_{xy}$  orbitals, which lie in the *xy* plane and interact with the five equatorial ligands. The  $d_{z^2}$  orbital energy will lie in the middle, because its interaction is primarily with the two axial lignds, with a more minor interaction between the annular part and the five equatorial ligands. The following CFT splitting scheme results:

MOs can be formed between the seven  $\sigma$ -SALCs from the ligands and the *d* orbitals from the metal, whose symmetries we have already determined. The following  $\Gamma_{SALC}$  can be generated:

Systematic reduction gives  $\Gamma_{SALC} = 2A_1' + E_1' + E_2' + A_2''$ . [Note that in carrying out the systematic reduction, 2 cos 72° = 0.6180 and 2 cos 144° = -1.6180, so the arithmetic is much cleaner than one might anticipate.] One of the two  $A_1'$  SALCs (with all positive wave function signs) could interact to make bonding and anti-bonding MOs with the *ns* orbital on the central metal, and the other (with all positive signs in the equatorial positions and negative signs in the two axial positions) will form bonding and antibonding combinations with the  $d_{z^2}$  orbital on the metal. The  $E_1'$  SALC pair has no match in *d* orbitals and must be strictly nonbonding, as is the case for the  $A_2''$  SALC. The  $E_2'$  pair of SALCs forms bonding and antibonding MOs with the  $d_{x^2-y^2}$ ,  $d_{xy}$  degenerate pair of orbitals, which have the same symmetry. The  $d_{xz}$ ,  $d_{yz}$  ( $e_1''$ ) pair on the metal have no symmetry match with SALCs and must remain nonbonding. As we have seen previously, seven pairs of electrons from the ligands would fill the lowest bonding and nonbonding levels [ $2\sigma$  ( $a_1'$ ),  $\sigma''$  ( $e_1''$ ),  $\sigma$  ( $e_2'$ ),  $\sigma''$  ( $a_2''$ ), not necessarily in that order]. Adding electrons from the metal would begin filling at the  $e_1'''$  level, a pair of nonbonding MOs, followed by successive filling of the  $a_1'$  and  $e_2'$  levels, which are antibonding MOs. Once again, the symmetries, energy order, and electron filling of the MOs above those accounting for ligand electron contributions are the same as predicted by the CFT approach. Only their identities as nonbonding and antibonding MOs are different.