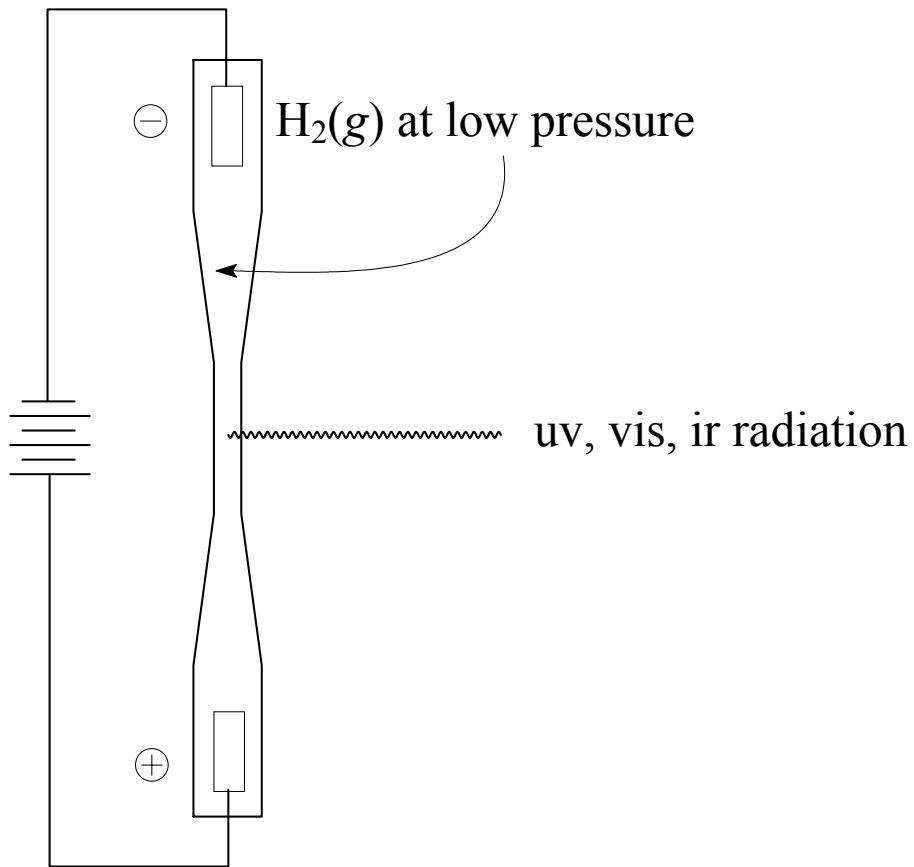


# Hydrogen Discharge Tube



Balmer Series (visible light):

- 656.3 nm (red)
- 486.1 nm (blue)
- 434.0 nm (indigo)
- 410.1 nm (violet)

@  
@  
@

# Balmer Equation for the Visible Line Spectrum of Hydrogen

Johann Balmer - 1885

$$\nu = U \left( \frac{1}{4} - \frac{1}{n^2} \right) \quad n = 3, 4, 5, \dots$$

$$U = \text{Rydberg constant} = 3.29 \times 10^{15} \text{ s}^{-1}$$

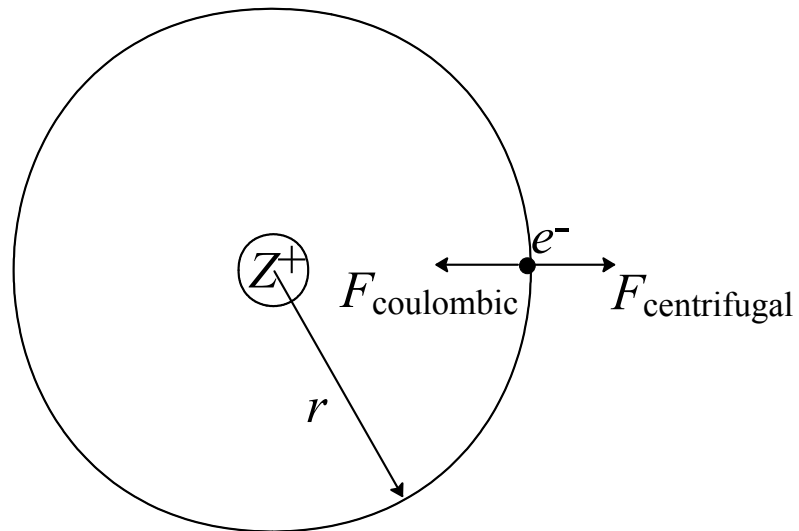
## Bohr's Model of the Atom

1. Electrons can have only certain fixed states of motion about the nucleus, and each state has a corresponding fixed energy.
2. Atoms radiate energy as electromagnetic radiation *only* through a transition from a high energy state to a lower energy state.
3. Electrons move in circular paths in any fixed state.
4. Allowed states of electron motion are those for which the angular momentum,  $mvr$ , is a multiple of  $h/2\pi$ . This is the *quantum hypothesis*:

$$mvr = nh/2\pi \quad n = 1, 2, 3, \dots$$

where  $n$  is the quantum number of the state.

# Counterbalancing Forces in the Bohr Model



$$F_{\text{centrifugal}} = -mv^2/r$$
$$F_{\text{coulombic}} = -Ze^2/r^2$$

## Predicted Relationships from Bohr's Model

Radius of an orbit:

$$r = \frac{n^2 h^2}{4\pi^2 m Z e^2} \quad n = 1, 2, 3, \dots$$

L When  $Z = 1$  (hydrogen) and  $n = 1$  (lowest state)  
 $r = 0.529 \text{ \AA} = a_0$ , called the Bohr radius.

L In terms of  $a_0$ ,

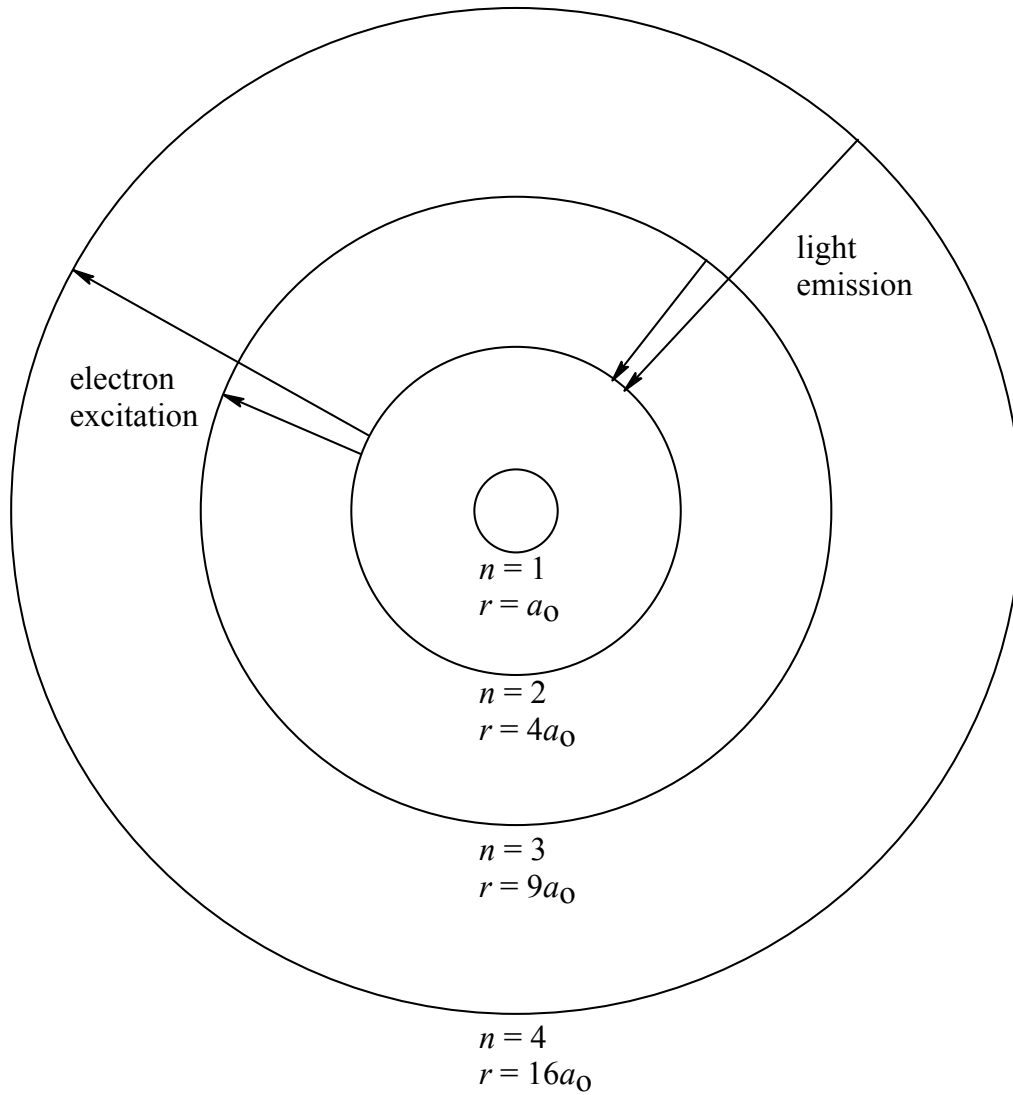
$$r = n^2 a_0 / Z$$

Energy of a state:

$$E = \frac{-2\pi^2 m Z^2 e^4}{n^2 h^2} = \frac{-BZ^2}{n^2}$$

# The Bohr Model of the Balmer Series

(Not to scale)



## Energy of Light Emitted in a Transition Between Energy States

$$E_{\text{light}} = E_{\text{final}} - E_{\text{initial}} = E_{\text{low}} - E_{\text{high}}$$

$$E_{\text{light}} = \frac{BZ^2}{n_{\text{low}}^2} - \frac{BZ^2}{n_{\text{high}}^2} = BZ^2 \left[ \frac{1}{n_{\text{low}}^2} - \frac{1}{n_{\text{high}}^2} \right]$$

But  $E = h\nu$ , so

$$\nu = \frac{BZ^2}{h} \left[ \frac{1}{n_{\text{low}}^2} - \frac{1}{n_{\text{high}}^2} \right]$$

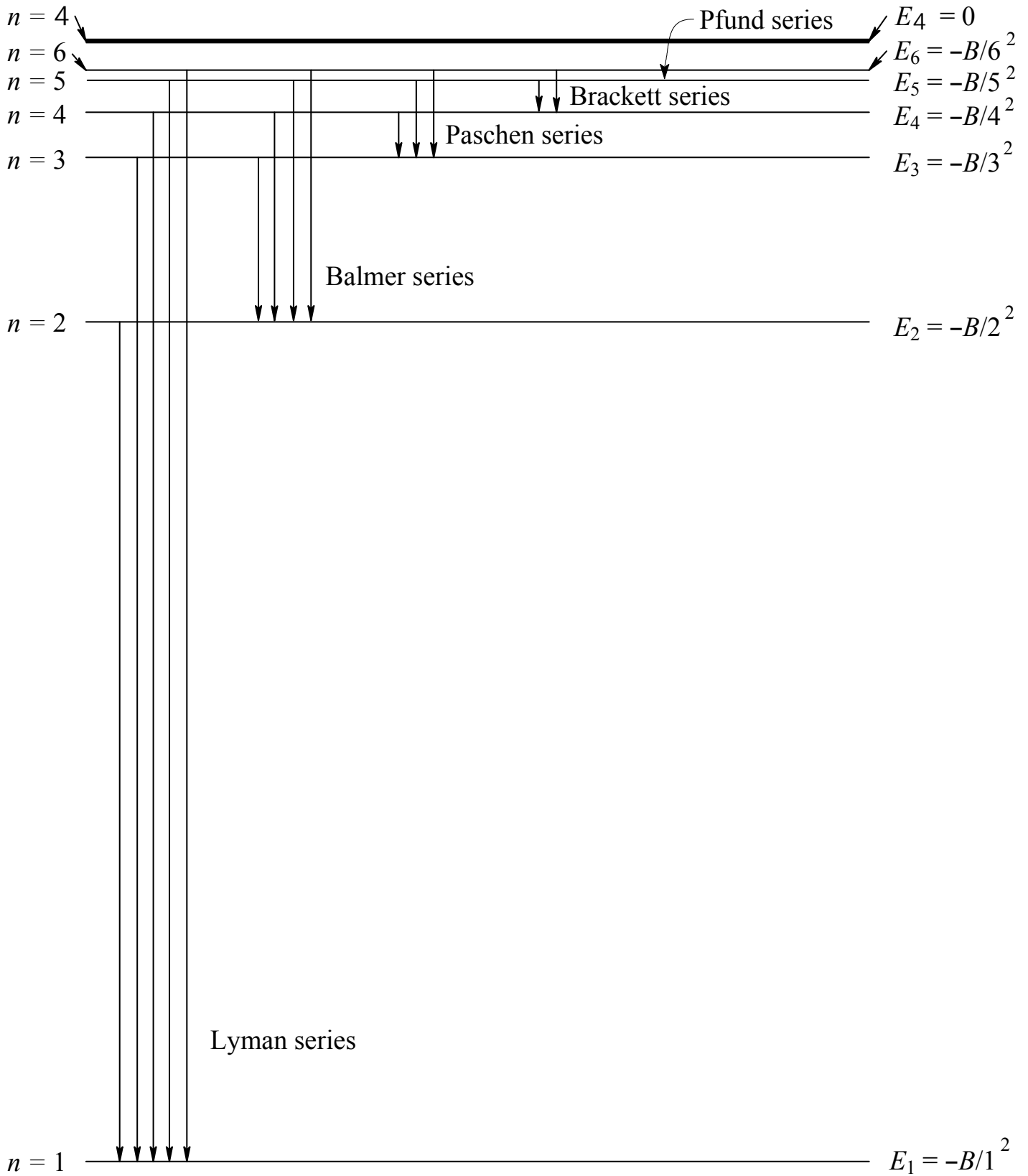
where  $BZ^2/h = U$ , the Rydberg constant. For the Balmer series, then

$$\nu = \frac{BZ^2}{h} \left[ \frac{1}{2^2} - \frac{1}{n_{\text{high}}^2} \right] = U \left[ \frac{1}{4} - \frac{1}{n_{\text{high}}^2} \right]$$

## Series of Line Spectra for Hydrogen Predicted by the Bohr Equation

$n_{\text{low}}$	$n_{\text{high}}$	Region	Series Name
1	2, 3, ..., 4	ultraviolet	Lyman
2	3, 4, ..., 4	visible	Balmer
3	4, 5, ..., 4	infrared	Paschen
4	5, 6, ..., 4	infrared	Brackett
5	6, 7, ..., 4	infrared	Pfund

# Energy Level Diagram for the Hydrogen Atom



## Problems With The Bohr Model

The ability to predict the frequencies of these series gave credibility to the Bohr model. But it had a number of limitations that lead to its complete abandonment by about 1935:

1. It could not satisfactorily explain the spectra of multi-electron atoms, even with extensive mathematical modification.
2. It could not explain the characteristic appearances of some lines in the various series, which spectroscopists routinely labeled with the following notations:  
 $s = \text{sharp}$   
 $p = \text{principal}$   
 $f = \text{fundamental}$   
 $d = \text{diffuse}$
3. It was fundamentally inconsistent with some newly discovered principles of physics.